# A numerical analysis of the influence of material properties on dry powder coating performance 

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#### Abstract

Dry powder coating is a preferable surface modification technique over the traditional aqueous coating technique due to reduced energy waste and less environmental impact. Despite the benefits of dry powder coating, excessive amount of coating powder energy input is often applied to ensure sufficient coating is achieved. In this study, the Discrete Element Method (DEM) is utilised to assess the influence of material properties on dry coating efficiency in a blade-driven system. Granular Bond number is used to predict coating performance based on multiple simulations with varied material properties. This provides insight on the optimal range of material properties (size ratio, density ratio and surface energy) to achieve uniformly distributed coatings, thus providing precise control of the quantity of coating material required and minimising energy consumption.


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## 1. Introduction

Dry powder coating has been widely used as a surface modification technique to create particles with desired functionalities or manufacturability such as enhanced flowability, by reducing separation distance between host particles, and controlled release of pharmaceutical drugs. The dry coating process is favourable over the conventional solventbased coating due to zero emission of volatile organic solvents and lower energy consumption as the subsequent drying process is not required, thus reducing processing time and costs. Moreover, dry coating is suitable for moisture sensitive Active Pharmaceutical Ingredients (APIs). Various techniques have been used for the dry deposition of guest particles onto the surface of host particles such as

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electrostatic coating (Jaber et al., 2021; Jing et al., 2022; Yang et al., 2015), mechanofusion (Qu et al., 2015; Zhou et al., 2010, 2011), hybridizer (Yang et al., 2005), rotating tumbler (Gärtner et al., 2021), resonance acoustic mixing (Kunnath et al., 2021), magnetic-assisted impact coating (Chen et al., 2010; Pfeffer et al., 2001; Yang et al., 2005), milling (Capece et al., 2021; Karde et al., 2015; Mullarney et al., 2011; Wei et al., 2017; Zhang et al., 2009), fluidised bed (Smikalla et al., 2011), high shear mixing (Karde et al., 2023) and pan coating (Fulchini et al., 2017). Detailed reviews of the different techniques are provided by Sharma and Setia (2019), Sauer et al. (2013) and Pfeffer et al. (2001). For the high shear processes, the dry coating process involves mechanical breakage and dispersion of agglomerates, collision with other particles and subsequent adhesion of fine (guest) particles onto the surface of carrier (host) particles. The deagglomeration of guest particles is primarily governed by the interparticle forces such as surface energy and van der Waals forces. As such, the mechanical energy imparted on the powder bed results in high shear stresses, which promote the breakage of agglomerates and dispersion of primary guest particles. Repeated high
impact collisional forces promote the adhesion of the guest particles onto the surface of host particles until the desired mixture homogeneity or surface area coverage is achieved by forming a discrete, continuous or film surface layer on the host particles. Despite the proven success of dry powder coating in many industrial applications, excessive amount of coating powder and energy input are typically required to achieve desired coating uniformity, where all target particles are sufficiently coated. Therefore, fundamental understanding of the factors governing dry powder coating is required to improve the process efficiency.

Several numerical studies have been carried out to elucidate the dry powder coating mechanisms (Alonso et al., 1989; Dave et al., 2003; Deng et al., 2018; Nguyen et al., 2016, 2014; Tamadondar et al., 2018). Tamadondar et al. (2018) carried out a DEM study on dry powder coating in a Couette cell and related the coating efficiency to the Stokes number and the ratio of cohesive to adhesive strength of particle contacts. Alonso et al. (1989) proposed a population balance model correlating particle size ratio and guest concentration to the coating quality. Although these models give some insight into the interplay between some material properties and the dry coating efficiency, more robust models are required for better understanding of the relative influence of material properties on the uniformity of dry coatings. The present study aims to examine the influence of size ratio, density ratio and surface energy on dry powder coating efficiency in a bladed high shear mixer by utilizing the Discrete Element Method (DEM to give insight on the optimal combination of material properties that give uniformly distributed coatings.

## 2. Methodology

The dry powder coating process was simulated using the Hertz-Mindlin-JKR model in the EDEM ${ }^{\ominus}$ software (Altair Engineering Inc.). In the Hertz-Mindlin-JKR contact model (Johnson et al., 1971), the contact normal force is given by,
$f_{n}=\frac{4 E^{*} a^{3}}{3 R^{*}}-\sqrt{8 \pi \Gamma E^{*} a^{3}}$
where $\Gamma$ is the interfacial energy, $a$ is the radius of normal contact area, $E^{*}$ and $R^{*}$ are the equivalent Young's modulus and particle radius given by Eqs. (2) and (3), respectively.
$E^{*}=\left(\frac{1-\nu_{i}^{2}}{E_{i}}+\frac{1-v_{j}^{2}}{E_{j}}\right)^{-1}$
$R^{*}=\frac{R_{i} R_{j}}{R_{i}+R_{j}}$
where $v_{i}, v_{j}$ are the Poisson's ratios, $E_{i}, E_{j}$ are the Young's moduli, and $R_{i}, R_{j}$ are the radii of the contacting particles. The normal overlap is given by,
$\delta=\frac{a^{2}}{R^{*}}-\sqrt{\frac{4 \pi \Gamma a}{E^{*}}}$
The dry coating system consists of a 25 mm diameter vessel and a 23.5 mm diameter impeller (with an inclination towards the tip) of the FT4 powder rheometer. A pre-segregated granular bed of host and guest particles was created by initially generating host particles with a bed height of 13 mm . A bed height of 13 mm was selected based on the swept volume by the blade such that there are no significant dead zones below and above the blade, which has a maximum vertical height of 6.14 mm . Thereafter, guest particles of $2 \%$


Fig. 1 - Geometries and bed configuration used in the simulations.
w/w concentration are generated and collected on a circular plate positioned at 0.5 mm above the host particles to form a thin layer of guest particles. The circular plate is then removed to allow the thin layer of guest particles to settle on the upper free layer of host particles under gravity as illustrated in Fig. 1. The impeller is rotated in a fixed vertical position at a rotational speed of 244 rpm for a duration of 5 blade revolutions. The material and interaction properties used in the simulations are given in Table 1. The effects of material properties (size ratio, density ratio and surface energy) on the surface area coverage (SAC) are evaluated. A minimum particle size ratio of 10 is investigated since particle size ratios less than 10 are unlikely for a dry coating process.

The SAC is defined as the ratio of the total projected area of guest particles to the maximum available host surface area, expressed as,
$S A C=\frac{1}{N_{h}} \sum_{n=1}^{N_{h}} \frac{n_{g} A_{p, g}}{\xi S_{h}} \times 100$
where $N_{h}$ is the total number of host particles, $n_{g}$ is the number of guest particles per host particle, $A_{p, g}$ is the projected area of the guest particles, $S_{h}$ is the surface area of the host particle, the factor $\xi=0.906$ (Thue, 1910) represents the highest density hexagonal packing arrangement of the spherical guest particles i.e., the maximum available surface area for coating. The maximum achievable SAC in an ideal system with uniformly distributed coatings i.e., ratio of total projected area of guest particles to total available surface area of host particles, given by
$\mathrm{SAC}_{\text {max }}=\frac{\sum_{i=1}^{N_{g}} r_{g, i}^{2}}{\sum_{j=1}^{N_{h}} 4 \xi r_{h, j}^{2}}$
To allow comparison to ideal coating, surface area coverage (Eq. 5) is normalised by the maximum achievable SAC (Eq. 6). The granular Bond number, Bo, is defined as the ratio of cohesive forces to the gravitational forces, expressed as,

Bo $=\frac{f_{c}}{f_{w}}$
where $f_{c}$ is the cohesive force between two particles according to the JKR contact theory (Johnson et al., 1971), given by Eq. (8) and $f_{w}$ is the harmonic mean of the gravitational forces given by Eq. (9).

| Property | Value |
| :---: | :---: |
| Mean guest diameter (mm) | 0.05-0.2 $\pm 5 \%$ |
| Mean host diameter (mm) | 0.5-2 $\pm 5$ \% |
| Particle density (kg/m ${ }^{3}$ ) | 2500-10000 |
| Geometry density ( $\mathrm{kg} / \mathrm{m}^{3}$ ) | 7800 |
| Particle Poisson's ratio (-) | 0.25 |
| Geometry Poisson's ratio (-) | 0.3 |
| Young's modulus (GPa) | 0.05 |
| Particle-particle sliding friction coefficient (-) | 0.3 |
| Particle-geometry sliding friction coefficient (-) | 0.2 |
| Particle-particle rolling friction coefficient (-) | 0.01 |
| Particle-geometry rolling friction coefficient (-) | 0.01 |
| Particle-particle restitution coefficient (-) | 0.8 |
| Particle-geometry restitution coefficient (-) | 0.9 |
| Particle-particle surface energy, $\Gamma\left(\mathrm{mJ} / \mathrm{m}^{2}\right)$ | 43-129 |
| Particle-geometry surface energy, $\Gamma\left(\mathrm{mJ} / \mathrm{m}^{2}\right)$ | 0 |

$f_{c}=\frac{3 \pi R^{*} \Gamma}{2}$
$f_{w}=\frac{2 w_{g} w_{h}}{w_{g}+w_{h}}$
where $w_{g}$ and $w_{h}$ are the weights of the contacting guest and host particles.

## 3. Results and discussion

### 3.1. Influence of size ratio

Fig. 2 shows the influence of the absolute particle size on the evolution of $\mathrm{SAC}_{\text {norm }}$ for systems with $r_{h} / r_{g}=10, \rho_{h}=\rho_{g}$ $=2500 \mathrm{~kg} / \mathrm{m}^{3}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$. For $r_{g} \leq 0.05 \mathrm{~mm}, \mathrm{SAC}_{\text {norm }}$ increases with number of blade revolutions and approaches a steady state. For $r_{g}=0.06 \mathrm{~mm}$ and $0.065 \mathrm{~mm}, \mathrm{SAC}_{\text {norm }}$ initially increases before reducing, suggesting that some guest particles that initially coat the hosts are dislodged upon further agitation. For $r_{g}>0.065 \mathrm{~mm}, \mathrm{SAC}_{\text {norm }}$ decreases with number of blade revolutions indicating poor coating. The initial $\mathrm{SAC}_{\text {norm }}$ is non-zero for $r_{g}>0.065 \mathrm{~mm}$, which can be attributed to percolation of guest particles during the vessel filling process before the blade rotation is initiated. This percolation phenomenon was much less significant for $r_{g} \leq 0.065 \mathrm{~mm}$, with decreasing significance for smaller host/guest particles. This can be observed by lower values of initial $\mathrm{SAC}_{\text {norm }}$ for smaller host/guest particles. Since the size ratio and interface energy are the same in all cases, the prevalence of this percolation problem, and subsequently the coating performance, is dictated by the granular Bond number shown in Fig. 3. For the purposes of defining a threshold for coating performance, we define cases where SAC $_{\text {norm }}$ initially increases to be good coating, and cases where it decreases to be poor coating. On this basis, from Fig. 2 the coating performance is classified to transition from good to poor for $0.065 \mathrm{~mm}<r_{g}<0.075 \mathrm{~mm}$, which corresponds to Bo $=160-212$. This range of Bo is considered to be the critical threshold, above and below which good and poor coating occur, respectively. It can be observed in Fig. 3 that Bo is predominantly influenced by guest particle size, with host


Fig. 2 - Evolution of SAC with mixing time for $r_{h} / r_{g}=10$ with different absolute particle size of guest and host particles where $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$ and $\rho_{\mathrm{h}}=\rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$.


Fig. 3 - Effect of guest particle size on granular Bond number between host and guest particles according to Eq. 7 where $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$ and $\rho_{h}=\rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$.
size having negligible effect. This can be explained by Eqs. 3, $7-9$, whereby $f_{w}, \mathrm{R}^{*}$ and subsequently $f_{c}$ are more strongly influenced by guest particle size.

Fig. 4 shows the influence of particle size ratio on the evolution of $\mathrm{SAC}_{\text {norm }}$ for fixed host particle sizes of 0.5 and 1.0 mm where $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$ and $\rho_{h}=\rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$. For size ratios $r_{h} / r_{g}=10$ and 20 , where $r_{h}=0.5 \mathrm{~mm}, \mathrm{SAC}_{\text {norm }}$ increases with number of blade revolutions, signifying good coating. However, there is a subsequent decrease of SAC $_{\text {norm }}$ after 5 blade revolutions for $r_{h} / r_{g}=10$, suggesting excessive energy input leads to detachment of guest particles from host surface. The rate of increase in $\mathrm{SAC}_{\text {norm }}$ is greater for $r_{h} / r_{g}=10$ than $r_{h} / r_{g}=20$, this is despite the greater Bond number for the latter ( $B 0=359$ and 1503, respectively). This is due to the smaller guest particles for $r_{h} / r_{g}=20$ being more cohesive, thus requiring a greater force to separate them from each other and disperse them.

For size ratios $r_{h} / r_{g}=10$ and 15 , where $r_{h}=1.0 \mathrm{~mm}$, $\mathrm{SAC}_{\text {norm }}$ decreases with number of blade revolutions indicating poor coating performance, whereas, for $r_{h} / r_{g}=17.5$ and $20, \mathrm{SAC}_{\text {norm }}$ initially increases with number of blade revolutions, which indicates good coating performance. The


Fig. 4 - Effect of particle size ratio on $S_{\text {SACm }}$ for (a) $r_{h}=0.5 \mathrm{~mm}$ and (b) $r_{h}=1.0 \mathrm{~mm}$ where $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$ and $\rho_{\mathrm{h}}=\rho_{\mathrm{g}}=2500 \mathrm{~kg} / \mathrm{m}^{3}$.
subsequent decrease in $\mathrm{SAC}_{\text {norm }}$ for $r_{h} / r_{g}=17.5$ and 20 suggests that segregation occurs due to guest detachment from host surfaces, caused by the excess energy input. For $r_{h} / r_{g}$ $=17.5$ and 20 , Bo $=285$ and 376 , respectively, which exceed the minimum threshold for good coating performance ( $160<$ Bo < 212). However, for $r_{h} / r_{g}=10$ and 15, poor coating performance is observed since $\mathrm{Bo}=90$ and 208, respectively, which fall below or within the threshold limit.

Fig. 5 shows the probability density of $S A C_{\text {norm }}$ for different size ratios after 5 blade revolutions. A slightly greater variance of SAC is observed for $r_{h} / r_{g}=10$ (where $r_{h}=0.5 \mathrm{~mm}$ ) than for $r_{h} / r_{g}=20$, which suggests more uniformly distributed coatings at $r_{h} / r_{g}=20$ albeit with similar proportion of uncoated host particles for both size ratios. For $r_{h}=1.0 \mathrm{~mm}$, a greater proportion of host particles are coated at $r_{h} / r_{g}=20$ than at $r_{h} / r_{g}=10$ due to better mixing and adherence of guest particles to host surfaces as shown by the distribution of
guest particles depicted in Fig. 6. For $r_{h} / r_{g}=10$, most of the guest particles settle and accumulate at the bottom of the vessel due to poor adhesion to host particles.

### 3.2. Influence of density ratio

Fig. 7 shows the effect of density ratio, expressed as ratio of guest particle density to host particle density, on the evolution of $\mathrm{SAC}_{\text {norm }}$ for $\rho_{h}=2500 \mathrm{~kg} / \mathrm{m}^{3}, r_{h}=0.5 \mathrm{~mm}, r_{g}=0.05 \mathrm{~mm}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$. For $\rho_{g} / \rho_{h}<1, \mathrm{SAC}_{\text {norm }}$ increases with increasing density ratio whereas for $\rho_{g} / \rho_{h}>1, \mathrm{SAC}_{\text {norm }}$ decreases with increasing density ratio. The ratio of cohesive forces to gravitational forces is much higher for the cases with $\rho_{g} / \rho_{h}<1$ as indicated by the granular Bond number in Fig. 8, as such the dominant interparticle forces reduce the dispersion rate and consequently, the coating rate. For $\rho_{g} / \rho_{h}$ $=1, \mathrm{SAC}_{\text {norm }}$ increases with number of blade revolutions up

Fig. 5 - Distribution of $\mathrm{SAC}_{\text {norm }}$ for different size ratios where (a) $r_{h}=0.5 \mathrm{~mm}$ and (b) $r_{h}=1.0 \mathrm{~mm}$ for $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$ and $\rho_{\mathrm{h}}=\rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$.

(a) $r_{h} / r_{g}=10$

(b) $r_{h} / r_{g}=15$

(c) $r_{h} / r_{g}=17.5$

(d) $r_{h} / r_{g}=20$

Fig. 6 - Distribution of guest particles for different size ratios after 5 blade revolutions for $r_{h}=1.0 \mathrm{~mm}, \Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$ and $\rho_{h}=\rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$.


Fig. 7 - Effect of density ratio on $\mathrm{SAC}_{\text {norm }}$ for $\rho_{\mathrm{h}}=2500 \mathrm{~kg} / \mathrm{m}^{3}$, $r_{h}=0.5 \mathrm{~mm}, r_{g}=0.05 \mathrm{~mm}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$.
to a maximum of unity before plateauing, indicating good coating performance. The plateauing of $\mathrm{SAC}_{\text {norm }}$ indicates good coating stability. The coating performance becomes progressively poorer with an increase of density ratio beyond


Fig. 8 - Effect of density ratio on granular Bond number according to Eq. 7 for $\rho_{\mathrm{h}}=2500 \mathrm{~kg} / \mathrm{m}^{3}, r_{h}=0.5 \mathrm{~mm}$ and Г mJ/m ${ }^{2}$.
unity. Fig. 8 shows that the granular Bond number for $\rho_{g} / \rho_{h}$ $=2$ is 180, which falls within the threshold limit of $160<$ Bo $<212$, and thus explains the short duration of the steady-state period (coating stability) before the subsequent decrease in SAC. The granular Bond number for $\rho_{g} / \rho_{h}=3$ and 4 is below the threshold limit and the transient peak SAC reached is not maintained. The short-lived transient peak SAC is caused by the initial bed dilation as the blades begin to rotate leading to instantaneous guest dispersal and percolation through the bed. Since the ratio of cohesive forces to gravitational forces is much lower in these cases, guest particles are very weakly adhered to host surfaces and therefore are easily and rapidly detached from the host surfaces upon further bed agitation.

For very dense guest particles, axial dispersion is faster due to increased gravitational forces, therefore, the percolation rate is higher as indicated by the greater magnitude of axial particle velocities for higher particle densities in Fig. 9. The distribution of $\mathrm{SAC}_{\text {norm }}$ for different density ratios is shown in Fig. 10. Lower density ratios exhibit more homogeneous distribution of $\mathrm{SAC}_{\text {norm }}$ than higher density ratios due to better mixing. This is clearly demonstrated in Fig. 11,


Fig. 9 - Variation of mean axial velocity of guest particles with density ratio for $\rho_{h}=2500 \mathrm{~kg} / \mathrm{m}^{3}, r_{h}=0.5 \mathrm{~mm}, r_{g}=0.05 \mathrm{~mm}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$.


Fig. 10 - Distribution of SAC for different density ratios for $\rho_{h}=2500 \mathrm{~kg} / \mathrm{m}^{3}, r_{h}=0.5 \mathrm{~mm}, r_{g}=0.05 \mathrm{~mm}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$.
which shows that a greater proportion of guest particles segregate to the bottom of the vessel at higher density ratios after 5 blade revolutions.

### 3.3. Influence of surface energy

Fig. 12 shows the effect of surface energy on $\mathrm{SAC}_{\text {norm }}$ for different density ratios where $\rho_{h}=2500 \mathrm{~kg} / \mathrm{m}^{3}, r_{h}=0.5 \mathrm{~mm}, r_{g}$ $=0.05 \mathrm{~mm}$. For $\rho_{g} / \rho_{h}=1$, the rate of increment of $\mathrm{SAC}_{\text {norm }}$ decreases with increasing surface energy. This behaviour can be partially attributed to the increase in the cohesive interparticle contact forces (see Fig. 13(a)) thus requiring higher shear stress or prolonged mixing time to break up and disperse the guest agglomerates. Furthermore, the increased $S A C_{n o r m}$ for lower surface energies is due to guest particle agglomerates being more easily dispersed leading to more free guest particles being available to coat the hosts. This is indicated in Fig. 13(b), which shows that for lower surface energies the number of guest-guest contacts are reduced.

Fig. 12 also shows that for $\rho_{g} / \rho_{h}=2$, doubling the surface energy from 43 to $86 \mathrm{~mJ} / \mathrm{m}^{2}$ improves the coating as the segregation phenomenon is mitigated due to stronger affinity of guest particles to host surfaces. This remains the case even for excess energy input, as SAC $_{\text {norm }}$ approaches unity after 3 blade revolutions and does not decrease with further revolutions. However, a further increase in the surface energy to $129 \mathrm{~mJ} / \mathrm{m}^{2}$ leads to a decrease in $\mathrm{SAC}_{\text {norm }}$ due to the guests being more difficult to disperse. Similarly, for $\rho_{g} / \rho_{h}=3$ and 4 , a surface energy of $43 \mathrm{~mJ} / \mathrm{m}^{2}$ leads to poor coating performance, whereas surface energies of 86 and $129 \mathrm{~mJ} / \mathrm{m}^{2}$ provide good coating performance. This suggests that for a given granular system, there exists a threshold range of surface energies, in which optimum coating performance is achieved; if the surface energy is too low the guests exist as discrete free particles and easily bypass the hosts or easily detach from host surfaces and percolate through the bed, whereas if surface energy is too high deagglomeration and dispersal of guests requires much more energy input and the coating process is slow.

### 3.4. Influence of size distribution

Guest and host particles with various size distributions were simulated for $\rho_{h}=\rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$. In these cases, a Gaussian distribution with the same mean particle sizes ( $r_{h}=0.5 \mathrm{~mm}, r_{g}=0.05 \mathrm{~mm}$ ) but varying values of standard deviation as a fraction of the mean, $\sigma$, are used, as shown in Fig. 14. Fig. 15 shows the effect of host and guest size distribution on SAC ${ }_{\text {norm }}$. For a normal Gaussian distribution of host particle size with $\sigma_{h}=0.1$, there is an apparent decrease in $\mathrm{SAC}_{\text {norm }}$ in comparison to the case with $\sigma_{h}=0.05$ and $\sigma_{9}=0.05$. This can be attributed to a $1.5 \%$ increase in available host surface area for coating. For a wider distribution of host particle size ( $\sigma_{h}=0.3$ ), there is an even greater reduction in $\mathrm{SAC}_{\text {norm }}$ by approximately $14 \%$ in comparison to the case with $\sigma_{h}=0.05$ and $\sigma_{g}=0.05$, which correspond to a $6.9 \%$ increase in available host surface area. For the case with $\sigma_{h}=0$ and $\sigma_{g}=0.1$, the total guest projected area increases by $0.7 \%$ relative to the case with $\sigma_{h}=0$ and $\sigma_{g}=0.05$, hence an increase in $\mathrm{SAC}_{\text {norm }}$. However, similar evolution of $\mathrm{SAC}_{\text {norm }}$ is observed for the cases where both guest and host particles have polydispersity and the cases where only the host particles have

(a) $\rho_{g} / \rho_{h}=1$

(b) $\rho_{g} / \rho_{h}=2$

(c) $\rho_{g} / \rho_{h}=3$

(d) $\rho_{g} / \rho_{h}=4$

Fig. 11 - Distribution of guest particles for different density ratios for $\rho_{h}=2500 \mathrm{~kg} / \mathrm{m}^{3}, r_{h}=0.5 \mathrm{~mm}, r_{g}=0.05 \mathrm{~mm}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$.


Fig. 12 - Effect of interfacial energy on SAC for $\rho_{h}=2500 \mathrm{~kg} / \mathrm{m}^{3}, r_{h}=0.5 \mathrm{~mm}$ and $r_{g}=0.05 \mathrm{~mm}$.
polydispersity. This is due to a relatively greater increase in total host surface area in contrast to the total guest projected area for the same variance. It can therefore be concluded that guest particle size distribution has limited effect on coating performance, whereas increased polydispersity of the hosts worsens the coating performance.

3.5. Coating performance based on granular Bond number

Fig. 16 shows granular Bond number as a function of size and density ratios, where only the guest particle size (monodisperse) and density are varied for $\rho_{\mathrm{h}}=2500 \mathrm{~kg} / \mathrm{m}^{3}$ and $\Gamma$


Fig. 13 - (a) Average guest-host contact forces as a function of surface energy and (b) evolution of guest-guest contacts for a range of surface energies for $r_{h}=0.5 \mathrm{~mm}, r_{g}=0.05 \mathrm{~mm}$ and $\rho_{h}=\rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$.


Fig. 14 - Particle size distribution of the simulated guest and host particles.


Fig. 15 - Effect of size distribution on SAC $_{\text {norm }}$ for $r_{h}$ $=0.5 \mathrm{~mm}, r_{g}=0.05 \mathrm{~mm}, \rho_{\mathrm{h}}=\rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$.


Fig. 17 - Granular Bond number as a function of particle size ratio and density ratio for $r_{g}=0.05 \mathrm{~mm}, \rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$.
$=43 \mathrm{~mJ} / \mathrm{m}^{2}$. Granular Bond numbers beyond the transition range of $160<B o<212$ represent good coating performance as previously discussed in Sections 3.1-3.3. The coloured circular markers represent the simulation results, where the shades represent the maximum $\mathrm{SAC}_{\text {norm }}$ achieved after 5 blade revolutions. The threshold range for Bo, represented by the black solid lines, appears to adequately define the regions of good and poor coating, as confirmed by the simulation results, where $\mathrm{SAC}_{\text {norm }}$ is typically $<0.65$ for the Bo values below the threshold and $>0.7$ above the threshold for the finer particle system ( $r_{h}=0.5 \mathrm{~mm}$ ). For the coarser particle system ( $r_{h}=1 \mathrm{~mm}$ ), $\mathrm{SAC}_{\text {norm }}$ is typically $<0.3$ for the Bo values below the threshold and $>0.35$ above the threshold. This difference can be attributed to the number of particles in each system; the finer particle system has a greater number of guest and host particles and thus denser than the coarser particle system. Upon agitation, a greater number of particles in the coarser particle system become airborne resulting in greater bed dilation and percolation rate of guest particles, which reduces the likelihood of guest particles coating the host surfaces.

Fig. 17 shows granular Bond number as a function of size and density ratios, where only the host particle density and size are varied for $r_{g}=0.05 \mathrm{~mm}, \rho_{g}=2500 \mathrm{~kg} / \mathrm{m}^{3}$ and


Fig. 16 - Granular Bond number as a function of particle size ratio and density ratio for (a) $r_{h}=0.5 \mathrm{~mm}$ and (b) $r_{h}=1 \mathrm{~mm}$ at $\rho_{h}$ $=2500 \mathrm{~kg} / \mathrm{m}^{3}$ and $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$.


Fig. 18 - Granular Bond number as a function of particle size ratio and density ratio for (a) $43 \mathrm{~mJ} / \mathrm{m}^{2}$, (b) $86 \mathrm{~mJ} / \mathrm{m}^{2}$ and (c) $129 \mathrm{~mJ} / \mathrm{m}^{2}$ at $r_{h}=0.5 \mathrm{~mm}$ and $\rho_{\mathrm{h}}=2500 \mathrm{~kg} / \mathrm{m}^{3}$.
$\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$. Significantly higher host density ratios $\rho_{g} /$ $\rho_{h}>40$ ) and size ratios ( $r_{h} / r_{g}>20$ ) are required for a notable change in the granular Bond number. This suggests that the guest particle size and density have a much greater effect on the granular Bond number in comparison to the host particle size and density. Fig. 18 shows granular Bond number as a function of size and density ratios for different surface energies and SAC ${ }_{\text {norm }}$ for several simulations with $r_{h}=0.5 \mathrm{~mm}$ and $\rho_{h}=2500 \mathrm{~kg} / \mathrm{m}^{3}$. For $\Gamma=43 \mathrm{~mJ} / \mathrm{m}^{2}$, the threshold range for Bo appears to adequately define the regions of good and poor coating, with $\mathrm{SAC}_{\text {norm }}>0.7$ above the threshold and $<0.7$ below the threshold. Increasing the surface energy improves coating performance for a given size and density ratio, however, for very high surface energies, the rate of increment of $\mathrm{SAC}_{\text {norm }}$ is reduced, as shown in Fig. 12.

It should be noted that the values of $\mathrm{SAC}_{\text {norm }}$ shown in Fig. 18 correspond only to the coating after 5 impeller revolutions, however in order to optimise dry coating processes it is important to consider the influence impeller speed and mixing time have on coating performance. This aspect will be addressed in further research. The validity of the model results shown in Figs. 16 and 18 can be scrutinized using literature data available on dry particle coating of pharmaceutical powders (Capece et al., 2014; Kunnath et al., 2021). The surface energy for host and guest materials was measured using Inverse Gas Chromatography (IGC). It is important to note that in the studies by (Capece et al., 2014) and (Kunnath et al., 2021), the cohesive force used for calculating the granular Bond number is based on the van der Waals force of attraction between host particles whereas in our work the cohesive force is calculated according to the JKR contact theory between host and guest particles (see Eqs. 7 and 8). For all cases investigated involving combinations of a range of pharmaceutical powders with silica, alumina and titania, good coating performance was achieved since Bo> $>212\left(10^{3}<\right.$ Bo $\left.<10^{11}\right)$.

## 4. Conclusions

Dry coating performance in a bladed mixer has been evaluated as a function of material properties. For a fixed size ratio, increasing the size of guest and host particles reduces the SAC due to poor sticking induced by the increase in
gravitational forces relative to cohesive forces for the guest particles. Increasing the span of distribution of host particles reduces $\mathrm{SAC}_{\text {norm }}$ due to an increase in the available total host surface area. Conversely, increasing the span of distribution of guest particles leads to an increase in $S A C_{n o r m}$ due to an increase in total projected area of guest particles. An increase in guest particle density reduces $S A C_{\text {norm }}$ due to the faster percolation of guests through the bed, and the greater adhesive force required for them to stick to host particles. $S A C_{n o r m}$ increases with surface energy when it is increased from a low value; however, very high surface energies negate the dispersibility of the agglomerated guest particles resulting in greater energy input being required to overcome the otherwise poor coating performance.

Granular Bond number, which dictates the affinity of guest particles to the surface of host particles, appears to provide an accurate characterisation of coating performance. Granular Bond number as a function of density and size ratios indicates that a threshold limit ( $160<B 0<212$ ) exists, above and below which good and poor coating occur, respectively. The guest particle size has a greater influence on the granular Bond number than the host particle size, hence a greater control of coating efficiency. It should be noted that this limit may depend on the operational parameters of the system.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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[^0]:    Abbreviations: DEM, Discrete Element Method; API, Active Pharmaceutical Ingredients; SAC, Surface Area Coverage; IGC, Inverse Gas Chromatography

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